

Chemistry 271, Section 21xx

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Your Name: Key

Your SID #: \_\_\_\_\_

General Chemistry and Energetics

Your Section #: \_\_\_\_\_

Exam I (100 points total)

March 7, 2011

$N = 184$

You have 50 minutes for this exam.

Exams written in pencil or erasable ink will not be re-graded under any circumstances.

Explanations should be concise and clear. I have given you more space than you should need. There is extra space on the last page if you need it.

You will need a calculator for this exam. No other study aids or materials are permitted.

Partial credit will be given, *i.e.*, if you don't know, guess.

Useful Equations:

$$K_a = [\text{H}^+][\text{A}^-]/[\text{HA}]$$

$$F = ma$$

$$K_w = [\text{H}^+][\text{HO}^-] = 10^{-14}$$

$$R = 0.08206 \text{ L}\cdot\text{atm}/\text{mole K}$$

$$K_p = K_c(RT)^{\Delta n}$$

$$\text{pH} = -\log([\text{H}^+])$$

$$e^{i\pi} + 1 = 0$$

$$\text{pH} = \text{p}K_a + \log([\text{A}^-]/[\text{HA}])$$

$$0^\circ\text{C} = 273.15 \text{ K}$$

$$P^2/\alpha^3 = 4\pi^2/MG$$

$$K_b = [\text{BH}^+][\text{HO}^-]/[\text{B}]$$

$$PV = nRT$$

$$\text{pH (e.p.)} = (\text{p}K_{a1} + \text{p}K_{a2})/2$$

$$\text{p}K_a = -\log(K_a)$$

$$\nabla \times E = -\partial B/\partial t$$

Honor Pledge: At the end of the examination time, please write out the following sentence and sign it, or talk to me about it:

"I pledge on my honor that I have not given or received any unauthorized assistance on this examination."

+1 point extra credit for filling in this box

## 1. (20 pts) Fill in the Blanks

Read the whole sentence before you fill in the blanks.

(a; 2 pts)  $K_c$  and  $K_p$  are equal if the number of moles of gas <sup>(+2)</sup> does not change during the reaction.

(b; 2 pts) The value of the reaction quotient  $Q$  approaches the equilibrium constant <sup>(+2)</sup> as the reaction progresses.

(c; 4 pts) At equilibrium, the rates of forward and reverse reactions are constant <sup>(+2)</sup> and are the same <sup>(+2)</sup> as each other.

(d; 4 pts) The conjugate base <sup>(+2)</sup> of a weak acid is a strong base whose  $pK_b$  can be predicted from the  $pK_a$  of the weak acid using the equation  $pK_b = 14 - pK_a$  or  $K_b = K_w / K_a$  <sup>(+2)</sup>

(e; 2 pts)  $K_w$  is the equilibrium constant for the water self-dissociation reaction <sup>(+2)</sup>

(f; 2 pts) The concentration of a solid or a pure liquid is constant as long as some of it is still present, so it is not included in <sup>(+2)</sup> the reaction quotient expression.

(g; 4 pts) Ideal gases are defined by two properties: the particles have no excluded volume <sup>(+2)</sup> and they do not <sup>(+2)</sup> attract each other.

**2. (28 pts) Chemical Equilibria [Adapted from Oxtoby].**

(a; 18 pts) Explain the effect of each of the following stresses on the position of the following equilibrium:



The reaction as written is exothermic (releases heat). In each case, briefly explain which way the equilibrium shifts and explain why. The five cases are independent of each other.

- (i)  $\text{N}_2\text{O}(g)$  is added to a mixture at equilibrium without changing the volume or the temperature.

(+3) Adding product  $\rightarrow$  drive equilibrium toward reactants  
LEFT

- (ii) The volume of the equilibrium mixture is reduced at constant temperature.

(+3) Pressure increases  $\rightarrow$  equilibrium shifts to reduce # of moles of gas  $\rightarrow$  shifts to the right

- (iii) The equilibrium mixture is cooled at constant volume.

(+3) for everyone ~~Unknownable - depends on exact values of  $\Delta H$  and  $T$~~

Questions (iv) and (v) are frequently answered incorrectly. Hint: Think about the  $Q$  and its ingredients.

- (iv) Gaseous argon (which does not react) is added to the equilibrium mixture and the total gas pressure and the temperature are maintained constant. (Hint: how would this be done?)

If the total pressure and  $T$  are constant, volume must be increasing

Therefore partial pressures drop. (+3)

$$Q = \frac{[\text{N}_2\text{O}][\text{NO}_2]}{[\text{NO}]^3} \quad \text{and the reaction shifts to}$$

increase total pressure of  $\text{N}_2\text{O}$ ,  $\text{NO}_2$ ,  $\text{NO}$

therefore shifts to the left (+3)

- (v) Gaseous argon is added to the equilibrium mixture without changing the volume or temperature.  
(Hint: what will the effect on  $Q$  be?)

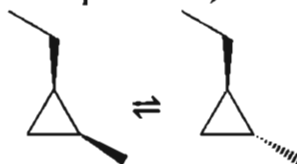
total pressure goes up but partial pressures do not change

$$Q = \frac{[NO_2][N_2O]}{[NO]^3} \text{ does not change } (+3)$$

T. rms

At equilibrium at 425.6 °C, a sample of *cis*-1-methyl-2-ethylcyclopropane is 73.6 % converted to the *trans* form (i.e. 73.6 % of the material is found in the *trans* form at equilibrium):

*cis*  $\rightleftharpoons$  *trans*



*cis* = 26.4%

- (b; 4 pts) Compute the equilibrium constant  $K$  for this reaction at 425.6 °C.

$$K = \frac{73.6}{26.4} = 2.79 \quad (+2)$$

- (c; 6 pts) Suppose that 0.525 mol of the *cis* compound is initially placed in a 15.0 L vessel and is then heated to 425.6 °C. Compute the equilibrium partial pressure of the *cis* and *trans* compounds. [Hint: you don't actually need the answer to part (b) to solve this.]

$$\text{Initial } P_{cis} = \frac{0.525 \text{ mol}}{15.0 \text{ L}} \cdot 0.08206 \text{ L}\cdot\text{atm/mol}\cdot\text{K} \cdot (425.6 + 273.15) \text{ K}$$

$$= 2.01 \text{ atm}$$

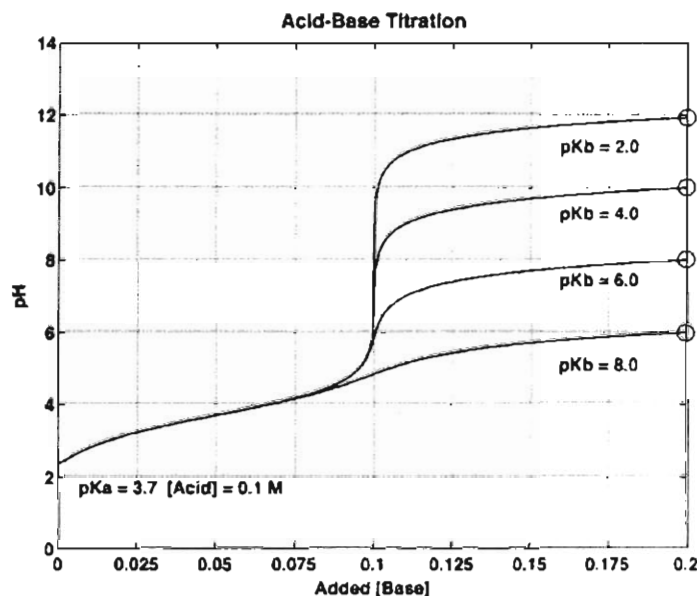
$$\text{So final } P_{trans} = 0.736 \times 2.01 = 1.48 \text{ atm} \quad (+2)$$

$$P_{cis} = 0.264 \times 2.01 = 0.530 \text{ atm} \quad (+2)$$

## 3. (22 pts) Acid-base equilibria

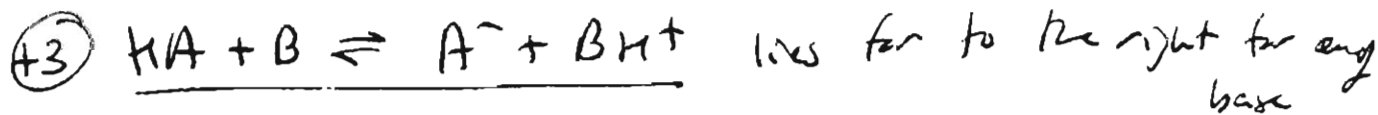
Consider four separate titrations of a weak acid HA ( $pK_a = 3.7$ ) with four different weak bases B2, B4, B6, and B8, with  $pK_b$ 's = 2, 4, 6, and 8 respectively.

The family of titration curves is shown in the graph at the right. The total concentration of acid is 0.1 M and the final concentration of base is 0.2 M. Ignore dilution.



(a; 6 pts) What is the dominant reaction occurring in the solution as HA and B are mixed?

Explain why all the titration curves look the same on the left half of the graph.



so the  $pK_b$  of the base doesn't make much difference to the amount of  $\text{A}^-$  we get

(b; 6 pts) When the final total concentrations of acid and base are 0.1 M and 0.2 M respectively, what are the concentrations  $[\text{B}]$  and  $[\text{BH}^+]$ , approximately (no ICE tables!). Using the base dissociation equilibrium, justify the circled pH values on the right hand side of the graph: show the calculation only once since it is the same for all of them.

(+3)  $[\text{B}] = 0.1 \text{ M}$   $[\text{BH}^+] = 0.1 \text{ M}$  because half of the base has reacted w/ HA to give  $\text{A}^- + \text{BH}^+$

(+3)  $K_b = \frac{[\text{BH}^+][\text{OH}^-]}{[\text{B}]}$  so  $[\text{OH}^-] = K_b \frac{[\text{B}]}{[\text{BH}^+]} = K_b$   
hence  $p\text{OH} = pK_b$   $pH = 14 - pK_b$

(c; 10 pts) The exact calculation of the titration curve of HA with B is complicated, especially at low concentrations of HA and B. We would like to solve for the six concentrations  $[HA]$ ,  $[A^-]$ ,  $[B]$ ,  $[BH^+]$ ,  $[H^+]$ , and  $[HO^-]$  given the  $K_a$  for HA, the  $K_b$  for B, and the input concentrations  $C_A$  and  $C_B$ . Write down the six equations that we would need to solve for the six variables.

$$(+1) [HA] + [A^-] = C_A$$

$$K_w = [H^+][HO^-] (+1)$$

$$(+1) [BH^+] + [B] = C_B$$

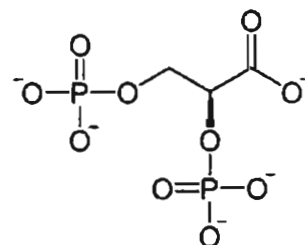
$$(+3) [H^+] + [BH^+] = [A^-] + [HO^-]$$

$$(+2) K_a = \frac{[H^+][A^-]}{[HA]}$$

$$(+2) K_b = \frac{[BH^+][HO^-]}{[B]}$$

### 3. (30 pts) Hemoglobin and Linkage

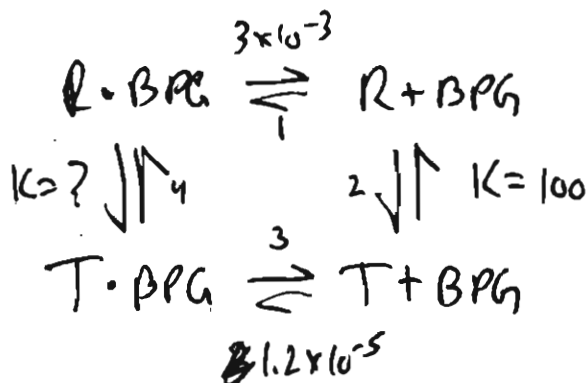
The molecule 2,3-bisphosphoglycerate (2,3-BPG) controls short-term adaptation to high altitude. It binds to T-state hemoglobin about 250-fold more tightly than it does to R-state hemoglobin. We know that the R and T states also interconvert.



(a; 8 pts) Given the three equilibria below, provide a linkage argument to show that the equilibrium constant for the interconversion of  $R \cdot BPG$  and  $T \cdot BPG$  is 25000.



Show that  $K_{RTBPG} = 25000$ :



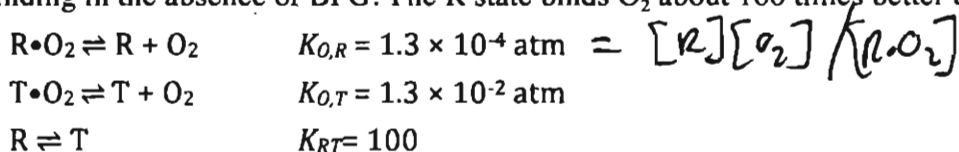
$$K_1 K_2 = K_4 K_3 (+3)$$

$$K_{RTBPG} = \frac{3 \times 10^{-3} \cdot 100}{1.2 \times 10^{-5}} = 25000$$

(+2) for calculation

(+3) for adding equilibria or writing square

(b; 12 pts) The mathematics of linkage is complicated. We will consider simplified cases. First, consider oxygen binding in the absence of BPG. The R state binds  $O_2$  about 100 times better than the T state:



If we find in the end that  $[R] = 1.5 \mu\text{M}$  and  $[O_2] = 2.6 \times 10^{-2} \text{ atm}$  (assumed constant) use the equilibria above to give the concentrations of  $R \cdot O_2$ ,  $T$ , and  $T \cdot O_2$ . The calculation is very straightforward: since I give you the equilibrium concentrations of  $R$  and  $O_2$  you do not need an ICE table.

$$\begin{aligned} R \cdot O_2 &\rightleftharpoons R + O_2 & [R \cdot O_2] &= \frac{[R][O_2]}{K_{O,R}} = 1.5 \mu\text{M} \cdot \frac{2.6 \times 10^{-2}}{1.3 \times 10^{-4}} = 300 \mu\text{M} \quad (+2) \\ (+2) \quad [T] &= K_{RT} [R] = 150 \mu\text{M} \quad (+1) \\ [T \cdot O_2] &= \frac{[T][O_2]}{K_{O,T}} = \frac{150 \mu\text{M} \cdot 2.6 \times 10^{-2}}{1.3 \times 10^{-2}} = 300 \mu\text{M} \quad (+1) \end{aligned}$$

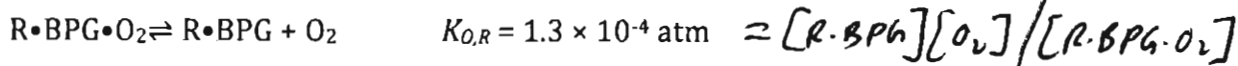
Calculate the fraction of the total hemoglobin that is bound to oxygen, i.e. calculate  $([R \cdot O_2] + [T \cdot O_2]) / ([R \cdot O_2] + [T \cdot O_2] + [R] + [T])$ .

$$\frac{[R \cdot O_2] + [T \cdot O_2]}{[R \cdot O_2] + [T \cdot O_2] + [R] + [T]} = \frac{600 \mu\text{M}}{600 + 1.5 + 150} = \frac{600}{751.5} = 79.8\% \quad (+2)$$

(+1) for idea of filling in from above  
(+1) for numbers

(79.8%)  
80%  
(+1)

(c; 10 pts) Next will consider the case when [BPG] is present, at high enough concentration so that all of the hemoglobin is in the BPG-bound form, and we will assess the effect of BPG on oxygen binding. We assume that the dissociation constants for the R and T states are the same with and without BPG.



Based on LeChatelier, circle whether more or less Hb is bound to  $O_2$  in the presence of BPG versus in its absence. If  $[R \cdot BPG] = 10 \text{ nM}$  and  $[O_2] = 2.6 \times 10^{-2} \text{ atm}$  (assumed constant) calculate the concentrations of  $R \cdot BPG \cdot O_2$ ,  $T \cdot BPG$ , and  $T \cdot BPG \cdot O_2$ . What fraction of the total hemoglobin is bound to oxygen?

$$[R \cdot BPG \cdot O_2] = \frac{[R \cdot BPG][O_2]}{K_{O,R}} = 10 \text{ nM} \times \frac{2.6 \times 10^{-2} \text{ atm}}{1.3 \times 10^{-4} \text{ atm}} = 2 \mu\text{M}$$

$$[T \cdot BPG] = K_{RTBPG} [R \cdot BPG] = 25000 \cdot 10 \text{ nM} = 250 \mu\text{M}$$

$$[T \cdot BPG \cdot O_2] = \frac{[T \cdot BPG][O_2]}{K_{O,T}} = 250 \mu\text{M} \cdot \frac{2.6 \times 10^{-2} \text{ atm}}{1.3 \times 10^{-2} \text{ atm}} = 500 \mu\text{M}$$

$$\% \text{ bound} = \frac{[R \cdot BPG \cdot O_2] + [T \cdot BPG \cdot O_2]}{[R \cdot BPG \cdot O_2] + [T \cdot BPG \cdot O_2] + [R \cdot BPG] + [T \cdot BPG]} = \frac{502}{502 + 0.01 + 250} = \frac{502}{752} = 67\%$$

Page	Score
1	/1
2	/20
3	/15
4	/13
5	/12
6	/18
7	/12
8	/10
<b>Total</b>	<b>/101</b>

Score for the page \_\_\_\_\_