| Chemistry 271, Section 22xx          | Your Name:      |                  |
|--------------------------------------|-----------------|------------------|
| Prof. Jason Kahn                     |                 |                  |
| University of Maryland, College Park | Your SID #:     |                  |
| General Chemistry and Energetics     | Your Section #: |                  |
| Exam II (100 points total)           |                 | November 7, 2011 |

You have 53 minutes for this exam.

Exams written in pencil or erasable ink will not be re-graded under any circumstances.

Explanations should be <u>concise</u> and <u>clear</u>. I have given you more space than you should need. There is extra space on the last page if you need it.

You will need a calculator for this exam. No other study aids or materials are permitted.

Partial credit will be given, *i.e.*, if you don't know, guess.

Useful Equations:

| $K_a = [H^+][A^-]/[HA]$   | $pH = -\log([H^+])$                                   | $K_b = [\text{HA}][\text{HO}^-]/[\text{A}^-]$                  |  |  |
|---|---|--|--|--|
| $K_w = [H^+][HO^-]$   | $pH = pK_a + \log [A^-]/[HA]$                         | $\Delta G^{\circ} = -RT \ln K_{eq}$                            |  |  |
| $R = 0.08206 \text{ L} \cdot \text{atm/mole K}$                 | 0 °C = 273.15 K                                       | $\ln K_{eq} = -\Delta H^{\circ} / (RT) + \Delta S^{\circ} / R$ |  |  |
| $\Delta S - q/T \ge 0$  | R = 8.314  J/mole  K = 1.98                           | 37 cal/mole K  |  |  |
| $S = k_B \ln W$   | $\Delta G = \Delta H - T \Delta S$                    | $E = \sum n_i \varepsilon_i$                                   |  |  |
| $W = N! / (\prod n_i!)$   | $n_i/n_0 = \exp[-(\varepsilon_i - \varepsilon_0)/kT]$ | $N = \sum n_i$   |  |  |
| $R = \mathbf{N}_A k_B$  | $k_B = 1.38 \text{ x } 10^{-23} \text{ J/K}$          | $t' = t - vx/c^2$  |  |  |
| Chemical standard state: 1 M solutes, pure liquids, 1 atm gases |   |  |  |  |

$$K_p = K_c (\text{RT})^{\Delta n}$$
  
 $P^2/a^3 = 4\pi^2/MG$   
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$   
Biochemical standard state: pH 7, all species in the ionic form found at pH 7  
nano:  $10^{-9}$   
pico:  $10^{-12}$   
zepto:  $10^{-21}$ 

Honor Pledge: At the end of the examination time, please write out the following sentence and sign it, or talk to me about it:

"I pledge on my honor that I have not given or received any unauthorized assistance on this examination."

+1 point extra credit for filling in this box

| 1. (15 pts) Short Answer   |         |  |  |  |
|--|---------|--|--|--|
| (2 pts each)<br>Fill in the blanks:  |         |  |  |  |
| The Boltzmann distribution describes the distribution of   | _ among |  |  |  |
| that is observed in each of the  |         |  |  |  |
| that comprise the predominant of the   | ,       |  |  |  |
| which is all of the microstates available at a given total   |         |  |  |  |
| (1 pt each) What is the sign of $\Delta G$ for any process that occurs spontaneously at constant P, T? |         |  |  |  |
| This a special case of the (circle one) First Law, Second Law, or Third Law of thermodynamics.         |         |  |  |  |
| The free energy has reached a minimum when a system has reached  |         |  |  |  |
|  |         |  |  |  |

## 2. (15 pts) van't Hoff

(a; 8 pts) Draw a van't Hoff plot for an endothermic disordering reaction. Label the axes, and show how you would determine  $\Delta H^{\circ}$  and  $\Delta S^{\circ}$  from the plot. If there is a region where the reaction is spontaneous, label it.

(b; 7 pts) From the van't Hoff equation, show that if you know the equilibrium constant at one temperature  $T_1$ , the equilibrium constant at temperature  $T_2$  is given by the following equation:

$$K_2 = K_1 \times \exp\left[\left(\frac{\Delta H^{\circ}}{R}\right)\left(\frac{1}{T_1} - \frac{1}{T_2}\right)\right]$$

#### 3. (20 pts) Boltzmann Distribution

(a; 6 pts) We often speak of "*k*T" as the energy available from thermal motion. What is the population relative to the ground state  $(n_i/n_0)$  of a state with an energy of *k*T above the ground state? What about a state with an energy of 10 *k*T?



# Boltzmann Distributions at Three Temperatures, N = 10000

(b; 6 pts) The temperatures of the three curves are 400, 800, and 1200 K. Indicate which temperature is which on the graph above, and how do you know?

(c; 2 pts) Identify the ground state populations for each distribution on the graph.

- (d; 3 pts) Sketch in the distribution for T = 1600 K.
- (e; 3 pts) Why are the areas under all four curves the same?

### 4. (30 pts) Practical Thermodynamics

(a; 25 pts) The water-gas shift reaction [CO (g) + H<sub>2</sub>O (g)  $\neq$  CO<sub>2</sub> (g) + H<sub>2</sub> (g)] is exothermic, which makes hydrogen production complicated because the syngas reaction that provides the feedstock is done at very high temperature. From the data in the table for 25 °C, calculate  $\Delta H^{\circ}_{rxn}$  and  $\Delta S^{\circ}_{rxn}$ . Assuming that  $\Delta H^{\circ}_{rxn}$ and  $\Delta S^{\circ}_{rxn}$  are constant with T, calculate the free energy change  $\Delta G^{\circ}_{rxn}$  at 200 °C, the equilibrium constant at 200 °C, and the temperature at which the equilibrium constant is equal to 1.

| $\Delta H^{\circ}_{f}$ in kJ/mol                             | S° in J/(mol K)                |
|--|--------------------------------|
| $\Delta H_{f}^{\circ}(CO) = -110.5$                          | S° (CO) = 197.7                |
| $\Delta H_{f}^{\circ}(CO_{2}) = -393.5$                      | $S^{\circ}(CO_2) = 213.6$      |
| $\Delta \mathrm{H}^{\circ}_{\mathrm{f}}(\mathrm{H}_{2}) = 0$ | $S^{\circ}(H_2) = 130.6$       |
| $\Delta H_{f}^{\circ}(H_{2}O, g) = -241.8$                   | $S^{\circ}(H_2O, g) = 188.8$   |
| $\Delta {\rm H}^{\circ}_{\rm f} ({\rm CH}_4) = -74.8$        | $S^{\circ}(CH_4) = 186.2$      |
| $\Delta H_{f}^{\circ}(C, graphite) = 0$                      | $S^{\circ}(C, graphite) = 5.7$ |
| $\Delta H^{\circ}_{f}(O_{2}) = 0$                            | $S^{\circ}(O_2) = 205$         |

(b; 5 pts) Why is choosing the temperature at which to carry out an exothermic reaction often a balancing act? Name another reaction that poses the same challenge.

### 5. (20 pts) Hemoglobin and Linkage

- Consider the competitive binding of chloride (Cl<sup>-</sup>) and oxygen (O<sub>2</sub>) to hemoglobin. We know that the R state of Hb binds O<sub>2</sub> better than the T state. We are told that Cl<sup>-</sup> binds better to the T state than to the R state.
- (6 pts) Draw the linkage cycle that shows that  $O_2$  binding favors the R state over the T state.

(6 pts) Draw the linkage cycle that shows that Cl<sup>-</sup> binding favors the T state.

(8 pts) Saturation with  $O_2$  in the lungs tend to drive  $Cl^-$  off Hb. Recalling that carbonic anhydrase is located in the red blood cell (RBC), how does chloride release help to accelerate the conversion of H<sup>+</sup> and bicarbonate back to  $CO_2$  and water so that the  $CO_2$  can be exhaled?

| Page  | Score |
|-------|-------|
| 1     | /1    |
| 2     | /23   |
| 3     | /13   |
| 4     | /14   |
| 5     | /25   |
| 6     | /17   |
| 7     | /8    |
| Total | /101  |