Chemistry 271, Section 23xx	Your Name:
Prof. Jason Kahn	
University of Maryland, College Park	Your SID #:
General Chemistry and Energetics	
Final Exam (200 points total)	Your Section # or time:

December 16, 2011

VIEWING: Monday, May 19, 9:30-10:30 a.m., Chem 1356-1360

You have 120 minutes for this exam.

Explanations should be <u>concise</u> and <u>clear</u>. There is extra space on the last page if you need it.

You will need a calculator for this exam. No other study aids or materials are permitted.

Generous partial credit will be given, *i.e.*, if you don't know, guess.

Useful Equations:

$K_a = [\mathrm{H}^+][\mathrm{A}^-]/[\mathrm{H}\mathrm{A}]$	$pH = -\log([H^+])$	$K_b = [HA][HO^-]/[A^-]$		
$K_w = [H^+][HO^-]$	$pH = pK_a + \log [A^-]/[HA]$	$\Delta G^{\circ} = -RT \ln K_{eq}$		
$R = 0.08206 \text{ L} \cdot \text{atm/mole K}$	$k_B = 1.38 \text{ x } 10^{-23} \text{ J/K}$	$\ln K_{eq} = -\Delta H^{\circ}/(RT) + \Delta S^{\circ}/R$		
$\Delta S - q/T \ge 0$	$R = 8.314 \text{ J/mole K} = 1.987 \text{ cal/mole K} = N_A k_B$			
$S = k_B \ln W$	$\Delta G = \Delta H - T \Delta S$	$E = \sum n_i \varepsilon_i$		
$W = N! / (\prod n_i!)$	$n_i/n_0 = \exp[-(\varepsilon_i - \varepsilon_0)/kT]$	$N = \Sigma n_i$		
Chemical standard state: 1 M solutes, pure liquids, 1 atm gases				
Biochemical standard state: pH 7, all species in the ionic form found at pH 7				
$^{\circ}C = ^{\circ}K - 273.15$	$P(v)dv = Cv^2 exp(-mv^2/2kT)$	$\mathbf{E} = \mathbf{E}^{\circ} - 2.303 (\mathbf{RT}/n\mathcal{F}) \log_{10} \mathbf{Q}$		
2.303 RT/ \mathcal{F} = 0.0592 Volts at 25 °C		\mathcal{F} = 96500 C(oulomb)/mole		
$\Delta G^{\circ} = -n \mathcal{F} E^{\circ}_{cell}$	$\ln k = (-E_a/RT) + \ln A$	1 Volt = 1 Joule/Coulomb		
$[\mathbf{A}] = [\mathbf{A}]_0 - kt$	$\ln[\mathbf{A}] = \ln[\mathbf{A}]_0 - kt$	$1/[A] = 1/[A]_0 + 2kt$		
Standard hydrogen electrode:	$2 \text{ H}^+(aq, 1 \text{ M}) + 2 e^- \rightarrow \text{H}_2$	(g) $E^{\circ} = 0.000 V$		

Honor Pledge: At the end of the examination time, please write out the following sentence and sign it, or talk to me about it:

"I pledge on my honor that I have not given or received any unauthorized assistance on this examination."

(+2 pts)

1. (24 pts) Multiple choice: Circle the single best answer for each question

(a; 4 pts) If the rate law for a process $A + B \rightarrow C$ is observed to be Rate = k[A][B]

- (1) the reaction must be an elementary reaction.
- (2) the reaction cannot be an elementary reaction.
- (3) the reaction might be an elementary reaction.
- (4) the experiment was done wrong.

(b; 4 pts) If the rate law for a process $A + B \rightarrow C + D$ is observed to be Rate = $k[A]^2/[C]$

- (1) the reaction must be an elementary reaction.
- (2) the reaction cannot be an elementary reaction.
- (3) the reaction might be an elementary reaction.
- (4) the experiment was done wrong.

(c; 4 pts) Cyclic reactions $A \rightarrow B \rightarrow C \rightarrow A$

- (1) are impossible.
- (2) can proceed in a net forward direction as drawn only if we heat the reaction to drive it.
- (3) at equilibrium, must also proceed in reverse at the same rate for each step.
- (4) None of the above.

(d; 4 pts) The melting temperature in DNA hybridization

- (1) increases with the number of mismatches between target and probe.
- (2) increases with the length of the complementary region.
- (3) increases as the concentration of DNA decreases.
- (4) None of the above.

(e; 4 pts) The lead-acid battery used in cars is so large and heavy because

- (1) the weight of the battery is needed to adjust the car's suspension.
- (2) it needs to store a lot of energy to recharge the alternator while driving.
- (3) it needs to have 60 internal cells to provide 120 V to the distributor and the car's electronics.
- (4) the starter motor requires high power and therefore current to move the pistons in the engine.

(f; 4 pts) Nitrogen fixation describes conversion of

- (1) N_2 to NH_3 .
- (2) NH₃ to NO_3^{-} .
- (3) NO_3^{-} to N_2 .
- (4) NH_3 to NO_3^{-} .

2. (48 pts) Kinetics, Rate Laws, and Arrhenius

$$N_2(g) + O_2(g) \rightarrow 2NO(g)$$

- The rate constant *k* for this reaction, which occurs during combustion as a precursor to NO₂ in smog formation, is 318 (units) at 2000 K and 7396 (units) at 2400 K. (Derived from Gilbert 15.85.)
- (a; 6 pts) Write down the rate law for the reaction assuming that it is elementary. What are the units for the rate constant?
- (b; 12 pts) Calculate the activation energy (Ea) and the pre-exponential factor (A) for the reaction.

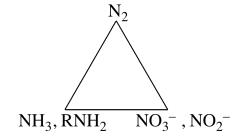
(c; 6 pts) Calculate the rate constant at 400 K. Given that NO is poisonous, it's a good thing the reaction is slow at anything close to room temperature.

(d; 12 pts) The half-life of ⁹⁰Sr, one of the main radioactive pollutants from the Fukushima and Chernobyl disasters, is 28.8 years. From the integrated rate equation for a first-order reaction, derive an expression for the half-life in terms of the rate constant, and calculate the rate constant for Sr-90 decay.

(e; 12 pts) Explain the functional form of the Maxwell-Boltzmann distribution $P(v)dv = Cv^2 exp(-mv^2/2kT)$. In other words, where do the v^2 and $exp(-mv^2/2kT)$ factors come from? Explain why doubling the temperature typically causes much more than a factor of 2 increase in the rate of elementary processes.

3. (40 pts) Electrochemistry of Life and the Biosphere

- The nitrogen triangle describes the interconversions among different oxidation states of nitrogen in the biosphere.
- (a; 6 pts) Is conversion of N_2 to NH_3 and amines a reduction or an oxidation? Is it assimilation or dissimilation?



(b; 9 pts) Denitrification is the reduction of nitrate to N₂. What might the reducing agent be, generically? What function is the nitrate serving? Is this assimilation or dissimilation?

(c; 9 pts) Nitrification refers to the oxidation of ammonia to nitrite or nitrate. Why do prokaryotes do this, assuming that they don't use nitrate for biomass? Why is this generally an aerobic process? What do we call the oxygen in aerobic nitrification?

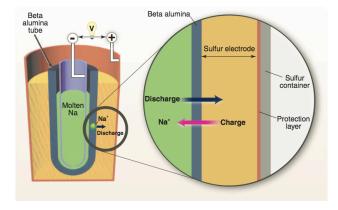
(d; 6 pts) Eukaryotes like us don't affect the nitrogen triangle very much (at least insofar as our personal metabolisms as opposed to industrial processes are concerned). Why not? What is the oxidation number of nitrogen in an amino acid, as at the right? HOOC— C_{α} —NH₂ (e; 10 pts) Why did the emergence of life on land have to wait for all the surface iron to be oxidized to rust?

4. (40 pts) Electrochemistry and Technology

The sodium-sulfur battery has been proposed as an energy storage component of the "smart grid." Sodium ions migrate through the beta alumina tube, but anions cannot go through it. Molten Na_2S_5 and molten S are immiscible liquids.

The relevant half-reactions are

$Na^+ + e^- \rightarrow Na(l)$	$E^{\circ}_{red} = -2.71 V$
$5 \text{ S}(l) + 2e^{-} \rightarrow \text{S}_5^{2-}$	$E^{\circ}_{red} = -0.48 V$



(a; 21 pts) Write down the overall reaction for the discharge part of the cycle (getting energy out of the battery), and calculate *n*. What is the composition of the molten sulfur electrode as the discharge progresses? The beta alumina tube is acting like a component of the simple beaker-based reactions we studied. Which component? How could you tell by just looking at the inside of the battery over time whether it was charging or discharging? Finally, why must water be rigorously excluded from the inside of the battery?

(b; 9 pts) Calculate E°_{cell} , ΔG° , and K_{eq} for the sodium-sulfur battery, all at 250 °C, assuming that the E°_{cell} is the same as it is at 25 °C. (The battery actually operates at about 250 °C to keep everything molten, which is why you are not likely to have one at home.)

(c; 10 pts) Energy storage in a smarter grid would allow for "load shifting," for example from mid-afternoon to nighttime. What does this mean and why is it a good idea?

5. (20 pts) SSA

The gas phase decomposition of NO₂Cl to give $2 \text{ NO}_2 + \text{Cl}_2$ was proposed to occur as follows:

 $NO_2Cl \Rightarrow NO_2 + Cl$ forward rate constant k_1 , backward k_{-1}

 $NO_2Cl + Cl \rightarrow NO_2 + Cl_2$ rate constant k_2

(a; 16 pts) Apply the SSA to the reactive chlorine atoms to show that the rate of appearance of Cl₂ should be

$$\frac{d[\operatorname{Cl}_2]}{dt} = \frac{k_1 k_2 [\operatorname{NO}_2 \operatorname{Cl}]^2}{k_{-1} [\operatorname{NO}_2] + k_2 [\operatorname{NO}_2 \operatorname{Cl}]}$$

(b; 4 pts) Under what conditions would you observe a rate that is first order with respect to NO₂Cl ?

6. (28 pts) Industrial electrochemistry

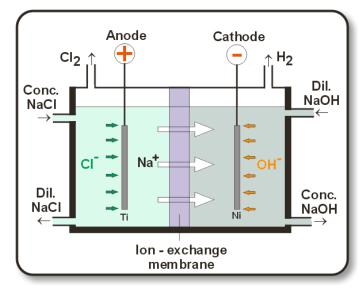
The Chloralkali process is the source of most chlorine gas and other oxidized forms of chlorine used for bleach etc. It is also a major player in Neal Stephenson's early science fiction novel *Zodiac*. The electrolysis process occurs under aqueous basic conditions.

Relevant half reactions are:

$\operatorname{Cl}_2(g) + 2 \ e^- \to 2 \ \operatorname{Cl}^-$	$E^{\circ}_{red} = +1.36 V$
$O_2(g) + 2 H_2O + 4 e^- \rightarrow 4 HO^-$	$E^{\circ}_{red} = +0.40 V$
$Na^+ + 1 e^- \rightarrow Na(s)$	$E^{\circ}_{red} = -2.71 V$
$2 \operatorname{H}_2\operatorname{O} + 2 e^- \longrightarrow \operatorname{H}_2(g) + 2 \operatorname{HO}^-$	$E^{\circ}_{red} = -0.83 V$

(a; 9 pts) Calculate E°_{cell} for each of the following

reactions. 2 Cl⁻ + 2 H₂O \rightarrow H₂ (g) + 2 HO⁻ + Cl₂ (g) 2 Cl⁻ + 2 Na⁺ \rightarrow 2 Na (s) + Cl₂ (g) 2 H₂O \rightarrow 2 H₂ (g) + O₂ (g)



(b; 6 pts) Calculate E_{cell} for $2 \operatorname{Cl}^- + 2 \operatorname{H}_2 O \rightarrow \operatorname{H}_2(g) + 2 \operatorname{HO}^- + \operatorname{Cl}_2(g)$ at 3 M NaCl, pH 11, 0.2 atm each gas.

(c; 13 pts) Explain why it is not surprising that solid Na is not produced from the electrolysis of brine, but it is surprising that we actually get any chlorine gas! What must be true of the electrochemistry occurring at the titanium anode? Where have we seen a very similar situation before? Give the balanced total reaction for the chloralkali cell.

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